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**Eric Bedford** and **Kyounghee Kim\*** ([kim@math.fsu.edu](mailto:kim@math.fsu.edu)), Department of Mathematics, FSU,  
Tallahassee, FL 32306. *Linear Fractional Recurrences: Periodicities and Integrability.*

We consider  $k$ -step recurrences of the form  $z_{n+k} = A(z)/B(z)$ , where  $A$  and  $B$  are linear functions of  $z_n, z_{n+1}, \dots, z_{n+k-1}$ , which we call  $k$ -step linear fractional recurrences. The first Theorem in this paper shows that for each  $k$  there are  $k$ -step linear fractional recurrences which are periodic of period  $4k$ . Among this class of recurrences, there is also the so-called Lyness process, which has the form  $A(z)/B(z) = (a + z_{n+1} + z_{n+2} + \dots + z_{n+k-1})/z_n$ . The second Theorem shows that the Lyness process has quadratic degree growth. The Lyness process is integrable, and we discuss its known integrals. (Received February 11, 2011)