# TAME AND WILD KERNELS OF QUADRATIC IMAGINARY NUMBER FIELDS 

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#### Abstract

For all quadratic imaginary number fields $F$ of discriminant $d>-5000$, we give the conjectural value of the order of Milnor's group (the tame kernel) $K_{2} O_{F}$, where $O_{F}$ is the ring of integers of $F$. Assuming that the order is correct, we determine the structure of the group $K_{2} O_{F}$ and of its subgroup $W_{F}$ (the wild kernel). It turns out that the odd part of the tame kernel is cyclic (with one exception, $d=-3387$ ).


## 1. Introduction

Assuming Lichtenbaum's conjecture one can compute conjectural values of orders of the tame kernels $K_{2} O_{F}$ of quadratic imaginary number fields $F$.

Since in general these orders are not very large, and there are several results known concerning the $p$-rank of $K_{2} O_{F}$ and of its subgroup $W_{F}$ called the wild kernel, it is possible to determine the structure of these groups for the fields in question with discriminants $d>-5000$.

## 2. Notations

We use the following notation.

- $\quad F$ is a number field with $r_{1}$ real and $2 r_{2}$ complex embeddings.
- $\zeta_{F}(s)$ is the Dedekind zeta function of $F$.
- $O_{F}$ is the ring of integers of $F$.
- $K_{n} O_{F}$ is the $n$th Quillen $K$-group of $O_{F}$, and especially
- $K_{2} O_{F}$ is the Milnor group of $O_{F}$ (the tame kernel).
- $W_{F}$ is the Hilbert kernel of $F$ (the wild kernel).
- $e_{p}$ is the $p-\operatorname{rank}$ of $K_{2} O_{F}$, where $p$ is a prime or $p=4$.
- $w_{2}$ is the $2-\mathrm{rank}$ of $W_{F}$.
- $\quad w(F)$ is the number of roots of unity in $F$.
- $C l(O)$ is the class group of a Dedekind ring $O$.
- $R_{m}(F)$ is a "twisted" version of the $m$ th Borel regulator (see [Bo1]), the "twisted" regulator map $r_{m}$ being a map

$$
r_{m}: K_{2 m-1} O_{F} \rightarrow\left[(2 \pi i)^{m-1} \mathbb{R}\right]^{d_{m}}
$$

[^0]where $d_{m}=r_{2}$ for $m$ even, and $d_{m}=r_{1}+r_{2}$ for odd $m>1\left(d_{m}\right.$ is just the order of vanishing of $\zeta_{F}(s)$ at $s=1-m$ ). The image of $r_{m}$ is a lattice of covolume $R_{m}(F)$-it differs from Borel's original one essentially by a power of $\pi$ ([Bo2]; there is also a shift $m \mapsto m+1$ compared to the original notation).

## 3. Computing the value $\# K_{2} O_{F}$

Borel proved that, up to a rational factor, $R_{m}(F)$ is equal to $\zeta_{F}^{*}(1-m)$, the first non-vanishing Taylor coefficient of $\zeta_{F}(s)$ at $s=1-m$. Lichtenbaum's conjecture [Li] (as modified by Borel [Bo1]) tries to interpret this rational factor and asks whether for all number fields and for any integer $m \geq 2$ there is a relation of the form

$$
\operatorname{res}_{s=1-m} \zeta_{F}(s)(s-1+m)^{-d_{m}(F)} \stackrel{?}{=} \pm \frac{\# K_{2 m-2}\left(O_{F}\right)}{\# K_{2 m-1}^{\mathrm{ind}}\left(O_{F}\right)_{\mathrm{tors}}} \cdot R_{m}(F)
$$

up to a power of 2 , where the subscript "tors" denotes the torsion part, "res" the residue, and "ind" the indecomposable part. $K_{2 m-2}\left(O_{F}\right)$ is known to be finite (Borel). There is some evidence for this conjecture, namely for $m=2$ and $F$ totally-real abelian it has been proved (up to a power of 2) by Mazur and Wiles $[\mathrm{M}-\mathrm{W}]$ as a consequence of their proof of the main conjecture of Iwasawa theory (in this case $R_{2}(F)=1$, though).

Recently Kolster, Nguyen Quang Do and Fleckinger ([KNF], Theorem 6.4) have proved a modified version of the conjecture (also up to a power of 2) for all abelian fields $F$ and $m \geq 2$. For imaginary quadratic fields $F$ and $m=2$, their result is equivalent to the above formula.

In what follows we assume $m=2$ and $F$ imaginary quadratic of discriminant $d$. In this case, the Lichtenbaum conjecture reads (using the functional equation for the zeta function and the fact that $\# K_{3}^{\text {ind }}\left(O_{F}\right)_{\text {tors }}$ is here always 24)

$$
\frac{3|d|^{3 / 2}}{\pi^{2} \cdot R_{2}(F)} \cdot \zeta_{F}(2) \stackrel{?}{=} \# K_{2}\left(O_{F}\right)
$$

up to a power of 2 .
Bloch [Bl] suggested and Suslin [Su] finally proved that Borel's regulator map can be given (at least rationally) in terms of the Bloch-Wigner dilogarithm $D_{2}(z)$ as a map on the Bloch group $\mathcal{B}(F)$; here $D_{2}(z)=\Im\left(L i_{2}(z)+\log |z| \log (1-z)\right)$, where $L i_{2}(z)=\sum_{n \geq 1} \frac{z^{n}}{n^{2}}$ is the classical dilogarithm function, defined for $|z|<1$ and analytically continued to $\mathbb{C}-[1, \infty)$, and $\mathcal{B}(F)$ is given in explicit form with generators and relations (cf. [Su]):

$$
\mathcal{B}(F)=\frac{\left\{\sum_{i} n_{i}\left[x_{i}\right] \mid \sum_{i} n_{i}\left(x_{i} \wedge\left(1-x_{i}\right)\right)=0 \in \bigwedge^{2} F^{\times}\right\}}{\left\langle\left.[x]-[y]+\left[\frac{y}{x}\right]-\left[\frac{1-y}{1-x}\right]+\left[\frac{1-y^{-1}}{1-x^{-1}}\right] \right\rvert\, x, y \in F^{\times}-\{1\}\right\rangle}
$$

The dilogarithm $D_{2}(z)$ maps $\mathcal{B}(F)$ into a lattice in $\mathbb{R}$ whose covolume we denote by $D_{2}^{F}$. Thus, we can replace $R_{2}(F)$ in the formula above by $D_{2}^{F}$ and still hope for the following equality to hold (up to a universal factor):

$$
\frac{3|d|^{3 / 2}}{\pi^{2} \cdot D_{2}^{F}} \cdot \zeta_{F}(2) \stackrel{?}{=} \# K_{2}\left(O_{F}\right)
$$

Note that in our formula we do not neglect powers of 2 .
The left hand side now can be computed numerically: we proceed by looking for elements $\xi \in \mathcal{B}(F)$ which are supported on exceptional $S$-units for some small
set $S$ of primes in $F$, i.e. $\xi=\sum_{i} n_{i}\left[x_{i}\right]$ such that $\sum_{i} n_{i}\left(x_{i} \wedge\left(1-x_{i}\right)\right)=0$, and the principal ideals $\left(x_{i}\right)$ and $\left(1-x_{i}\right)$ are generated by $S$. The images $D_{2}(\xi)$ lie in a 1-dimensional lattice, therefore the numerically computed values should all be commensurable. The covolume $D_{2}^{F, S}$ of this lattice is an integral multiple of $D_{2}^{F}$ (to be precise, the covolume that we actually get depends not only on $S$ but also on the bounds that we impose on the valuations $v_{\mathcal{P}}\left(x_{i}\right)$ for $\mathcal{P} \in S$ in our search). If we have obtained hundreds of different values $D_{2}(\xi)$ there is a good chance that they already generate the correct lattice $D_{2}(\mathcal{B}(F))$ and give $D_{2}^{F}$ exactly.

Our program, written in PARI [BBCO], performs the above calculations successively for an increasing set of primes and stops if the corresponding $D_{2}^{F, S}$ stabilizes, i.e. if the same covolume occurs for $S$ and $S^{\prime} \supsetneqq S$.

The orders in the case of small discriminants have been determined by Tate [Ta] (for $|d| \leq 15)$, Skałba $[S k](d=-19,-20)$, and Qin [Q2], [Q3] $(d=-24,-35)$, and they coincide with ours. Furthermore, the entries of a former (shorter) table [Ga] were not only compatible with the structural theoretical results known at the time but even suggested several conjectures, most of which have been proved in the meantime ([B-92], [C-H], [Q1]).

Our approach is very similar to that of Grayson [Gr], only we don't have to restrict ourselves to class number one, and our program works even for quite large discriminants (e.g., for $F=\mathbb{Q}(\sqrt{-2000004})$ we obtain $\left.\# K_{2} O_{F}=4\right)$.

The program is freely available from the second author via e-mail, together with some remarks on the modification of the parameters.

## 4. Determining the structure

In order to establish the actual structure of the tame and wild kernel we apply the following results: let $d^{\prime}=d / \operatorname{gcd}(4, d)$.
(1) The index $i_{F}:=\left(K_{2} O_{F}: W_{F}\right)$ always divides 6 . More precisely,

$$
\begin{array}{llc}
2 \mid i_{F} & \text { iff } & d^{\prime} \equiv \pm 1(\bmod 8), \\
3 \mid i_{F} & \text { iff } & d \equiv-3(\bmod 9), \quad d \neq-3
\end{array}
$$

(See [B-82], Table 1.)
(2) The 2-rank of the tame and wild kernels can be computed easily:

$$
e_{2}= \begin{cases}t, & \text { if every odd prime divisor of } d \text { is } \equiv \pm 1 \quad(\bmod 8) \\ t-1, & \text { otherwise },\end{cases}
$$

where $t$ is the number of odd prime divisors of $d$; and

$$
w_{2}= \begin{cases}e_{2}, & \text { if } d^{\prime} \not \equiv 1 \quad(\bmod 8) \\ e_{2}-1, & \text { otherwise }\end{cases}
$$

(See $[B-S]$, Theorem 4.)
(3) The 4-rank of the tame kernel can be easily determined using the results of [Q1], at least if the number of odd prime divisors of $d$ does not exceed 3 .

The $p$-rank of $K_{2} O_{F}$, for odd $p$, is related to the $p$-rank of the class group of an appropriate number field as follows.
(4) Let $E_{3}=\mathbb{Q}(\sqrt{-3 d})$ and $e_{3}^{\prime}=3$-rank $C l\left(O_{E_{3}}\right)$. Then

$$
e_{3}=e_{3}^{\prime}, \quad \text { if } d \not \equiv-3 \quad(\bmod 9),
$$

$$
\max \left(1, e_{3}^{\prime}\right) \leq e_{3} \leq e_{3}^{\prime}+1, \quad \text { otherwise }
$$

(See [B-92], Theorem 5.6.)
(5) Let $E_{5}=\mathbb{Q}(\sqrt{5 d})$, and $e_{5}^{\prime}=5$-rank $C l\left(O_{E_{5}}\right)$. Then $e_{5} \leq e_{5}^{\prime}$. (See [B-92], Theorem 5.4.)
(6) For $p>5$, where $p$ is a regular prime, let $E_{p}$ be the maximal real subfield of the field $F\left(\zeta_{p}\right)$, and let $e_{p}^{\prime}=p$-rank $C l\left(O_{E_{p}}\right)$. Then $e_{p} \leq e_{p}^{\prime}$. (See [B-92], Theorem 5.4.)

## 5. Examples

As above, let $d^{\prime}=d / \operatorname{gcd}(4, d)$.

1) For $d=-644$, we have $\# K_{2} O_{F}=32$ (conjecturally), and $e_{2}=2, w_{2}=2$. Moreover $e_{4}=1$, since $644=4 \cdot 7 \cdot 23$, and $7 \equiv 23 \equiv 7(\bmod 8)$, see [Q1]. Finally, $\left(K_{2} O_{F}: W_{F}\right)=2$, since $d^{\prime}=-161 \equiv 7(\bmod 8)$ and $d \not \equiv-3(\bmod 9)$. It follows that

$$
K_{2} O_{F}=\mathbb{Z} / 2 \times \mathbb{Z} / 16 \quad \text { and } \quad W_{F}=\mathbb{Z} / 2 \times \mathbb{Z} / 8
$$

2) For $d=-255$ we have $\# K_{2} O_{F}=12$ (conjecturally). Moreover $e_{2}=2, w_{2}=1$, and $d \equiv-3(\bmod 9)$. Therefore

$$
K_{2} O_{F}=\mathbb{Z} / 2 \times \mathbb{Z} / 2 \times \mathbb{Z} / 3 \quad \text { and } \quad W_{F}=\mathbb{Z} / 2
$$

3) For $d=-759$, we have $\# K_{2} O_{F}=36$ (conjecturally), and $e_{2}=2, \quad w_{2}=1$, and $d \equiv-3(\bmod 9)$. Moreover, for

$$
E_{3}=\mathbb{Q}(\sqrt{3 d})=\mathbb{Q}(\sqrt{-253})
$$

we have 3-rank $\mathrm{Cl}\left(O_{E_{3}}\right)=0$. Therefore

$$
K_{2} O_{F}=\mathbb{Z} / 2 \times \mathbb{Z} / 2 \times \mathbb{Z} / 9 \quad \text { and } \quad W_{F}=\mathbb{Z} / 2 \times \mathbb{Z} / 3
$$

4) For $d=-2395$, we have $\# K_{2} O_{F}=25$ (conjecturally). Moreover, for $E_{5}=$ $\mathbb{Q}(\sqrt{5 d})=\mathbb{Q}(\sqrt{-479})$, we have $5-\operatorname{rank} C l\left(O_{E_{5}}\right)=1$. Therefore, using (5),

$$
K_{2} O_{F}=W_{F}=\mathbb{Z} / 25
$$

5) For $d=-1832$, we have $\# K_{2} O_{F}=49$ (conjecturally). The maximal real subfield $E_{7}$ of the field $F\left(\zeta_{7}\right)=\mathbb{Q}\left(\sqrt{-d}, \zeta_{7}\right)$ is generated over $\mathbb{Q}$ by a root of the polynomial

$$
f(x)=x^{6}+7 d x^{4}+14 d^{2} x^{2}+7 d^{3}
$$

In our case

$$
e_{7}^{\prime}=7-\operatorname{rank} C l\left(O_{E_{7}}\right)=1
$$

Therefore, in view of (6),

$$
K_{2} O_{F}=W_{F}=\mathbb{Z} / 49
$$

## 6. Description of the table

In the first column there is the negative discriminant $d$. The last two columns give the structure of the tame and the wild kernel of the corresponding field. In these columns a single number $n$ denotes the cyclic group of order $n$, and a sequence $\left(n_{1}, n_{2}, \ldots\right)$ denotes the direct sum of cyclic groups of orders $n_{1}, n_{2}, \ldots$.

The last two columns contain correct results provided the conjectural value of $\# K_{2} O_{F}$ is correct.

Table 1. Table of tame and wild kernels for imaginary quadratic number fields of discriminant $d>-5000$ (conjectural values)

| $d$ | tame | wild | d | tame | wild | $d$ | tame | wild |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -3 | 1 | 1 | -163 | 1 | 1 | -328 | 2 | 2 |
| -4 | 1 | 1 | -164 | 4 | 2 | -331 | 3 | 3 |
| -7 | 2 | 1 | -167 | 2 | 1 | -335 | 2 | 1 |
| -8 | 1 | 1 | -168 | 2 | 2 | -339 | 2 | 2 |
| -11 | 1 | 1 | -179 | 1 | 1 | -340 | 2 | 2 |
| -15 | 2 | 1 | -183 | $(2,3)$ | 1 | -344 | 1 | 1 |
| -19 | 1 | 1 | -184 | 2 | 2 | -347 | 1 | 1 |
| -20 | 1 | 1 | -187 | 2 | 2 | -355 | 2 | 2 |
| -23 | 2 | 1 | -191 | 2 | 1 | -356 | 4 | 2 |
| -24 | 1 | 1 | -195 | $(2,2)$ | $(2,2)$ | -359 | 2 | 1 |
| -31 | 2 | 1 | -199 | 2 | 1 | -367 | $(2,3)$ | 3 |
| -35 | 2 | 2 | -203 | 2 | 2 | -371 | 2 | 2 |
| -39 | $(2,3)$ | 1 | -211 | 1 | 1 | -372 | $(2,3)$ | 2 |
| -40 | 1 | 1 | -212 | 1 | 1 | -376 | 2 | 2 |
| -43 | 1 | 1 | -215 | 2 | 1 | -379 | 1 | 1 |
| -47 | 2 | 1 | -219 | $(4,3)$ | 4 | -383 | 2 | 1 |
| -51 | 2 | 2 | -223 | 2 | 1 | -388 | 8 | 4 |
| -52 | 1 | 1 | -227 | 1 | 1 | -391 | $(2,2)$ | 2 |
| -55 | 2 | 1 | -228 | $(4,3)$ | 2 | -395 | 2 | 2 |
| -56 | 2 | 2 | -231 | $(2,2)$ | 2 | -399 | $(2,4,3)$ | 4 |
| -59 | 1 | 1 | -232 | 1 | 1 | -403 | 2 | 2 |
| -67 | 1 | 1 | -235 | 2 | 2 | -404 | 1 | 1 |
| -68 | 8 | 4 | -239 | 2 | 1 | -407 | 2 | 1 |
| -71 | 2 | 1 | -244 | 1 | 1 | -408 | $(2,3)$ | 2 |
| -79 | 2 | 1 | -247 | 2 | 1 | -411 | 2 | 2 |
| -83 | 1 | 1 | -248 | 2 | 2 | -415 | 2 | 1 |
| -84 | $(2,3)$ | 2 | -251 | 1 | 1 | -419 | 3 | 3 |
| -87 | 2 | 1 | -255 | $(2,2,3)$ | 2 | -420 | $(2,4)$ | $(2,2)$ |
| -88 | 1 | 1 | -259 | 2 | 2 | -424 | 1 | 1 |
| -91 | 2 | 2 | -260 | 4 | 2 | -427 | 2 | 2 |
| -95 | 2 | 1 | -263 | 2 | 1 | -431 | 2 | 1 |
| -103 | 2 | 1 | -264 | $(2,3)$ | 2 | -435 | $(2,2,3)$ | $(2,2)$ |
| -104 | 1 | 1 | -267 | 2 | 2 | -436 | 1 | 1 |
| -107 | 3 | 3 | -271 | 2 | 1 | -439 | 2 | 1 |
| -111 | $(2,3)$ | 1 | -276 | 2 | 2 | -440 | 2 | 2 |
| -115 | 2 | 2 | -280 | 2 | 2 | -443 | 1 | 1 |
| -116 | 1 | 1 | -283 | 1 | 1 | -447 | 2 | 1 |
| -119 | $(2,2)$ | 2 | -287 | $(2,2)$ | 2 | -451 | 2 | 2 |
| -120 | $(2,3)$ | 2 | -291 | $(4,3)$ | 4 | -452 | 8 | 4 |
| -123 | 2 | 2 | -292 | 4 | 2 | -455 | $(2,2)$ | 2 |
| -127 | 2 | 1 | -295 | 2 | 1 | -456 | 2 | 2 |
| -131 | 1 | 1 | -296 | 1 | 1 | -463 | 2 | 1 |
| -132 | 4 | 2 | -299 | 2 | 2 | -467 | 1 | 1 |
| -136 | 4 | 4 | -303 | $(2,11)$ | 11 | -471 | $(2,3)$ | 1 |
| -139 | 1 | 1 | -307 | 1 | 1 | -472 | 5 | 5 |
| -143 | 2 | 1 | -308 | 2 | 2 | -479 | $(2,7)$ | 7 |
| -148 | 1 | 1 | -311 | 2 | 1 | -483 | $(2,2)$ | $(2,2)$ |
| -151 | 2 | 1 | -312 | 2 | 2 | -487 | 2 | 1 |
| -152 | 1 | 1 | -319 | 2 | 1 | -488 | 1 | 1 |
| -155 | 2 | 2 | -323 | 4 | 4 | -491 | 13 | 13 |
| -159 | 2 | 1 | $-327$ | $(2,3)$ | 1 | -499 | 1 | 1 |

Table 1. (Continued)

| $d$ | tame | wild |
| :---: | :---: | :---: |
| -503 | $(2,3)$ | 3 |
| -511 | $(2,2)$ | 2 |
| -515 | 2 | 2 |
| -516 | $(4,3)$ | 2 |
| -519 | 2 | 1 |
| -520 | 2 | 2 |
| -523 | 1 | 1 |
| -527 | $(2,2)$ | 2 |
| -532 | 2 | 2 |
| -535 | 2 | 1 |
| -536 | 1 | 1 |
| -543 | $(2,3)$ | 1 |
| -547 | 1 | 1 |
| -548 | 4 | 2 |
| -551 | 2 | 1 |
| -552 | $(2,3)$ | 2 |
| -555 | $(2,2,7)$ | $(2,2,7)$ |
| -559 | 2 | 1 |
| -563 | 1 | 1 |
| -564 | 2 | 2 |
| -568 | 2 | 2 |
| -571 | 5 | 5 |
| -579 | $(4,3)$ | 4 |
| -580 | 4 | 2 |
| -583 | $(2,17)$ | 17 |
| -584 | 2 | 2 |
| -587 | 1 | 1 |
| -591 | 2 | 1 |
| -595 | $(2,2)$ | $(2,2)$ |
| -596 | 1 | 1 |
| -599 | 2 | 1 |
| -607 | 2 | 1 |
| -611 | 2 | 2 |
| -615 | $(2,2,3)$ | 2 |
| -616 | 2 | 2 |
| -619 | 1 | 1 |
| -623 | $(2,2)$ | 2 |
| -627 | $(2,2)$ | $(2,2)$ |
| -628 | 1 | 1 |
| -631 | 2 | 1 |
| -632 | 2 | 2 |
| -635 | 2 | 2 |
| -643 | 3 | 3 |
| -644 | $(2,16)$ | $(2,8)$ |
| -647 | 2 | 1 |
| -651 | $(2,2,3)$ | $(2,2)$ |
| -655 | 2 | 1 |
| -659 | 1 | 1 |
| -660 | $(2,2,3)$ | $(2,2)$ |
| -663 | $(2,2)$ | 2 |
| -664 | 1 | 1 |
|  |  |  |


| $d$ | tame | wild |
| :---: | :---: | :---: |
| -667 | 2 | 2 |
| -671 | 2 | 1 |
| -679 | $(2,2,5)$ | $(2,5)$ |
| -680 | 2 | 2 |
| -683 | 1 | 1 |
| -687 | $(2,3)$ | 1 |
| -691 | 1 | 1 |
| -692 | 1 | 1 |
| -695 | 2 | 1 |
| -696 | $(2,3,7)$ | $(2,7)$ |
| -699 | 2 | 2 |
| -703 | $(2,37)$ | 37 |
| -707 | 2 | 2 |
| -708 | 4 | 2 |
| -712 | 2 | 2 |
| -715 | $(2,2)$ | $(2,2)$ |
| -719 | 2 | 1 |
| -723 | $(4,3)$ | 4 |
| -724 | 1 | 1 |
| -727 | 2 | 1 |
| -728 | 2 | 2 |
| -731 | 4 | 4 |
| -739 | 1 | 1 |
| -740 | 4 | 2 |
| -743 | 2 | 1 |
| -744 | 2 | 2 |
| -751 | 2 | 1 |
| -755 | $(2,41)$ | $(2,41)$ |
| -759 | $(2,2,9)$ | $(2,3)$ |
| -760 | 2 | 2 |
| -763 | 2 | 2 |
| -767 | 2 | 1 |
| -771 | $(2,3)$ | $(2,3)$ |
| -772 | 8 | 4 |
| -776 | 4 | 4 |
| -779 | 2 | 2 |
| -787 | 1 | 1 |
| -788 | 1 | 1 |
| -791 | $(2,2)$ | 2 |
| -795 | $(2,2,3)$ | $(2,2)$ |
| -799 | $(2,4)$ | 4 |
| -803 | 2 | 2 |
| -804 | $(4,9)$ | $(2,3)$ |
| -807 | 2 | 1 |
| -808 | 1 | 1 |
| -8011 | 1 | 1 |
| -8115 | 2 | 1 |
| -815 | 4 | 4 |
| -820 | 2 | 1 |
| -823 | 2 | 2 |
| -824 | 1 | 1 |
| -827 | 1 |  |
|  |  |  |


| $d$ | tame | wild |
| :---: | :---: | :---: |
| -831 | $(2,3)$ | 1 |
| -835 | $(2,3)$ | $(2,3)$ |
| -836 | 4 | 2 |
| -839 | 2 | 1 |
| -840 | $(2,2,3)$ | $(2,2)$ |
| -843 | 2 | 2 |
| -851 | 2 | 2 |
| -852 | 2 | 2 |
| -856 | 1 | 1 |
| -859 | 1 | 1 |
| -863 | $(2,3)$ | 3 |
| -868 | $(2,4)$ | $(2,2)$ |
| -871 | 2 | 1 |
| -872 | 1 | 1 |
| -879 | $(2,5)$ | 5 |
| -883 | 1 | 1 |
| -884 | 4 | 4 |
| -887 | $(2,5)$ | 5 |
| -888 | 2 | 2 |
| -895 | 2 | 1 |
| -899 | 2 | 2 |
| -903 | $(2,2,3)$ | 2 |
| -904 | 4 | 4 |
| -907 | 1 | 1 |
| -911 | 2 | 1 |
| -915 | $(2,2)$ | $(2,2)$ |
| -916 | 1 | 1 |
| -919 | 2 | 1 |
| -920 | 2 | 2 |
| -923 | 2 | 2 |
| -932 | $(4,5)$ | $(2,5)$ |
| -935 | $(2,2)$ | 2 |
| -939 | $(4,3)$ | 4 |
| -943 | $(2,2)$ | 2 |
| -947 | 1 | 1 |
| -948 | $(2,3)$ | 2 |
| -951 | 2 | 1 |
| -952 | $(2,2)$ | $(2,2)$ |
| -955 | 2 | 2 |
| -959 | $(2,4)$ | 4 |
| -964 | 8 | 4 |
| -967 | 2 | 1 |
| -971 | 5 | 5 |
| -979 | 4 | 4 |
| -983 | 2 | 1 |
| -984 | $(2,3)$ | 2 |
| -987 | $(2,2)$ | $(2,2)$ |
| -991 | 2 | 1 |
| -995 | 2 | 2 |
| -996 | 4 | 2 |
| -1003 | 4 | 4 |
|  |  |  |

Table 1. (Continued)

| $d$ | tame | wild | d | tame | wild | $d$ | tame | wild |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -1007 | (2, 3) | 3 | -1171 | 1 | 1 | -1343 | (2, 2) | 2 |
| -1011 | $(4,3)$ | 4 | -1172 | 1 | 1 | -1347 | 2 | 2 |
| -1012 | 2 | 2 | -1187 | 7 | 7 | -1348 | 16 | 8 |
| -1015 | $(2,2)$ | 2 | -1191 | $(2,27)$ | 9 | -1351 | (2, 4) | 4 |
| -1016 | $(2,13)$ | $(2,13)$ | -1192 | 3 | 3 | -1355 | $(2,3)$ | $(2,3)$ |
| -1019 | 1 | 1 | -1195 | 2 | 2 | -1363 | 2 | 2 |
| -1023 | $(2,16)$ | 16 | -1199 | 2 | 1 | -1364 | 2 | 2 |
| -1027 | 2 | 2 | -1203 | 2 | 2 | -1367 | 2 | 1 |
| -1028 | 8 | 4 | -1204 | 2 | 2 | -1371 | $(4,3,5)$ | $(4,5)$ |
| -1031 | 2 | 1 | -1207 | $(2,2)$ | 2 | -1379 | 2 | 2 |
| -1032 | 2 | 2 | -1208 | $(2,3)$ | $(2,3)$ | -1380 | $(2,4,3)$ | $(2,2)$ |
| -1039 | 2 | 1 | -1211 | 2 | 2 | -1383 | 2 | 1 |
| -1043 | 2 | 2 | -1219 | 2 | 2 | -1384 | 1 | 1 |
| -1047 | $(2,3)$ | 1 | -1220 | 4 | 2 | -1387 | $(4,11)$ | $(4,11)$ |
| -1048 | $(3,11)$ | $(3,11)$ | -1223 | 2 | 1 | -1391 | 2 | 1 |
| -1051 | 1 | 1 | -1227 | $(4,3)$ | 4 | -1396 | 1 | 1 |
| -1055 | 2 | 1 | -1231 | 2 | 1 | -1399 | 2 | 1 |
| -1059 | 2 | 2 | -1235 | $(2,2,11)$ | $(2,2,11)$ | -1403 | 2 | 2 |
| -1060 | 4 | 2 | -1236 | $(2,9)$ | $(2,3)$ | -1407 | $(2,2,3)$ | 2 |
| -1063 | $(2,29)$ | 29 | -1239 | $(2,8)$ | 8 | -1411 | 4 | 4 |
| -1064 | 2 | 2 | -1240 | $(2,17)$ | $(2,17)$ | -1412 | 16 | 8 |
| -1067 | 4 | 4 | -1243 | $(4,7)$ | $(4,7)$ | -1415 | 2 | 1 |
| -1076 | 1 | 1 | -1247 | 2 | 1 | -1416 | (2, 3) | 2 |
| -1079 | 2 | 1 | -1252 | 4 | 2 | -1419 | $(2,2,9)$ | $(2,2,9)$ |
| -1087 | $(2,3)$ | 3 | -1255 | 2 | 1 | -1423 | 2 | ( 1 |
| -1091 | 1 | 1 | -1256 | 5 | 5 | -1427 | 3 | 3 |
| -1092 | (2, 4, 3) | $(2,2)$ | -1259 | 1 | 1 | -1428 | $(2,2)$ | $(2,2)$ |
| -1095 | $(2,2)$ | 2 | -1263 | $(2,3)$ | 1 | -1432 | 1 | 1 |
| -1096 | $(2,31)$ | $(2,31)$ | -1267 | 2 | 2 | -1435 | (2, 2) | $(2,2)$ |
| -1099 | 2 | , | -1268 | 1 | 1 | -1439 | 2 | 1 |
| -1103 | $(2,5)$ | 5 | -1271 | $(2,2)$ | 2 | -1443 | $(2,4,3)$ | $(2,4)$ |
| -1108 | 1 | 1 | -1272 | $(2,9)$ | $(2,3)$ | -1447 | , | 1 |
| -1111 | 2 | 1 | -1279 | 2 | 1 | -1448 | 3 | 3 |
| -1112 | 5 | 5 | -1283 | 5 | 5 | -1451 | 1 | 1 |
| -1115 | 2 | 2 | -1284 | 4 | 2 | -1455 | $(2,2)$ | 2 |
| -1119 | $(2,3)$ | 1 | -1288 | $(2,4)$ | (2, 4) | -1459 | 1 | 1 |
| -1123 | 1 | 1 | -1291 | 3 | 3 | -1460 | 2 | 2 |
| -1124 | 4 | 2 | -1295 | $(2,2)$ | 2 | -1463 | (2, 2) | 2 |
| -1128 | $(2,3)$ | 2 | -1299 | $(8,3)$ | 8 | -1464 | 2 | 2 |
| -1131 | $(2,2)$ | $(2,2)$ | -1303 | 2 | 1 | -1471 | $(2,7)$ | 7 |
| -1135 | $(2,7)$ | 7 | -1304 | 1 | 1 | -1479 | $(2,2,3)$ | 2 |
| -1139 | 4 | 4 | -1307 | 1 | 1 | -1480 | 2 | 2 |
| -1140 | (2, 2) | $(2,2)$ | -1311 | (2, 2) | 2 | -1483 | 1 | 1 |
| -1144 | 2 | 2 | -1315 | 2 | 2 | -1487 | $(2,5)$ | 5 |
| -1147 | 2 | 2 | -1316 | (2, 4) | $(2,2)$ | -1491 | $(2,2)$ | $(2,2)$ |
| -1151 | 2 | , | -1319 | $(2,3)$ | 3 | -1492 | 1 | 1 |
| -1155 | $(2,2,2,3)$ | $(2,2,2)$ | -1320 | $(2,2,13)$ | $(2,2,13)$ | -1495 | $(2,2,17)$ | $(2,17)$ |
| -1159 | 2 | 1 | -1327 | $(2,3)$ | 3 | -1496 | 2 | 2 |
| -1160 | 2 | 2 | -1335 | $(2,2,3)$ | 2 | -1499 | 1 | 1 |
| -1163 | 1 | 1 | -1336 | 2 | 2 | -1507 | 4 | 4 |
| -1167 | 2 | 1 | -1339 | 2 | 2 | -1508 | 4 | 2 |

Table 1. (Continued)

| d | tame | wild | $d$ | tame | wild | $d$ | tame | wild |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -1511 | 2 | 1 | -1671 | 2 | 1 | -1839 | $(2,3,5)$ | , |
| -1515 | $(2,2,9)$ | $(2,2,3)$ | -1672 | 2 | 2 | -1843 | $(2,3)$ | $(2,3)$ |
| -1523 | 7 | 7 | -1679 | $(2,4)$ | 4 | -1844 | 1 | 1 |
| -1524 | $(2,3)$ | 2 | -1684 | 1 | 1 | -1847 | $(2,23)$ | 23 |
| -1527 | 2 | 1 | -1687 | $(2,2)$ | 2 | -1848 | $(2,2,3)$ | $(2,2)$ |
| -1528 | 2 | 2 | -1688 | 1 | 1 | -1851 | 2 | 2 |
| -1531 | 1 | 1 | -1691 | $(2,3)$ | (2, 3) | -1855 | $(2,2)$ | 2 |
| -1535 | 2 | 1 | -1695 | $(2,2,3)$ | , | -1860 | $(2,4)$ | $(2,2)$ |
| -1540 | $(2,4)$ | $(2,2)$ | -1699 | , | 1 | -1864 | 2 | 2 |
| -1543 | 2 | , | -1703 | 2 | 1 | -1867 | 1 | 1 |
| -1544 | 4 | 4 | -1704 | $(2,3)$ | 2 | -1871 | $(2,3)$ | 3 |
| -1547 | $(2,2,3)$ | $(2,2,3)$ | -1707 | 2 | 2 | -1876 | 2 | 2 |
| -1551 | $(2,2,3)$ | , | -1711 | 2 | 1 | -1879 | $(2,3)$ | 3 |
| -1555 | , | 2 | -1716 | (2, 2) | $(2,2)$ | -1880 | 2 | 2 |
| -1556 | 1 | 1 | -1720 | , | , | -1883 | 2 | 2 |
| -1559 | 2 | 1 | -1723 | 7 | 7 | -1887 | $(2,2)$ | 2 |
| -1560 | $(2,2,3)$ | $(2,2)$ | -1727 | 2 | 1 | -1891 | 2 | 2 |
| -1563 | 2 | 2 | -1731 | $(4,3)$ | 4 | -1892 | 4 | 2 |
| -1567 | 2 | 1 | -1732 | 8 | 4 | -1895 | $(2,3)$ | 3 |
| -1571 | 7 | 7 | -1735 | $(2,5)$ | 5 | -1896 | 2 | 2 |
| -1572 | $(4,5)$ | $(2,5)$ | -1736 | $(2,2,7)$ | $(2,2,7)$ | -1903 | 2 | 1 |
| -1576 | , | , | -1739 | 2 | 2 | -1907 | 1 | 1 |
| -1579 | 1 | 1 | -1743 | $(2,4)$ | 4 | -1912 | 2 | 2 |
| -1583 | $(2,27)$ | 27 | -1747 | 1 | 1 | -1915 | 2 | 2 |
| -1588 | 3 | 3 | -1748 | 2 | 2 | -1919 | 2 | 1 |
| -1591 | 2 | 1 | -1751 | (2, 2) | 2 | -1923 | 2 | 2 |
| -1592 | 2 | 2 | -1752 | 4 | 4 | -1924 | 4 | 2 |
| -1595 | $(2,2)$ | $(2,2)$ | -1759 | 2 | 1 | -1927 | $(2,2)$ | 2 |
| -1599 | $(2,2)$ | 2 | -1763 | 4 | 4 | -1928 | 4 | 4 |
| -1603 | , | 2 | -1767 | $(2,2,3)$ | 2 | -1931 | 1 | 1 |
| -1604 | 8 | 4 | -1768 | 4 | 4 | -1939 | 2 | 2 |
| -1607 | 2 | 1 | -1771 | (2, 2) | $(2,2)$ | -1940 | 2 | 2 |
| -1608 | 2 | 2 | -1779 | 2 | 2 | -1943 | 2 | 1 |
| -1615 | $(2,2)$ | 2 | -1780 | 4 | 4 | -1947 | $(2,4,3)$ | $(2,4)$ |
| -1619 | , | 3 | -1783 | 2 | 1 | -1951 | $(2,3,5)$ | $(3,5)$ |
| -1623 | (2, 3) | 1 | -1784 | 2 | 2 | -1955 | $(2,2)$ | $(2,2)$ |
| -1624 | 2 | 2 | -1787 | 1 | 1 | -1956 | $(4,3)$ | , |
| -1627 | 1 | 1 | -1795 | 2 | 2 | -1959 | 2 | 1 |
| -1631 | $(2,2)$ | 2 | -1796 | $(8,7)$ | $(4,7)$ | -1963 | 2 | 2 |
| -1635 | $(2,2)$ | $(2,2)$ | -1799 | $(2,2)$ | 2 | -1967 | $(2,2,3)$ | $(2,3)$ |
| -1636 | $(4,19)$ | $(2,19)$ | -1803 | $(4,3,13)$ | $(4,13)$ | -1972 | 2 | 2 |
| -1639 | 2 | 1 | -1807 | 2 | , | -1976 | 2 | 2 |
| -1640 | 4 | 4 | -1811 | 1 | 1 | -1979 | 1 | 1 |
| -1643 | 2 | 2 | -1812 | $(2,3)$ | 2 | -1983 | $(2,3)$ | 1 |
| -1651 | 2 | 2 | -1816 | 1 | 1 | -1987 | 1 | 1 |
| -1652 | 2 | 2 | -1819 | 2 | 2 | -1988 | $(2,8)$ | $(2,4)$ |
| -1655 | 2 | 1 | -1823 | 2 | 1 | -1991 | 2 | 1 |
| -1659 | $(2,2,3)$ | $(2,2)$ | -1828 | 4 | 2 | -1992 | $(2,3)$ | 2 |
| -1663 | 2 | 1 | -1831 | 2 | 1 | -1995 | $(2,2,2)$ | $(2,2,2)$ |
| -1667 | 83 | 83 | -1832 | 49 | 49 | -1999 | 2 | , |
| -1668 | $(4,9)$ | $(2,3)$ | -1835 | 2 | 2 | -2003 | 1 | 1 |

Table 1. (Continued)

| $d$ | tame | wild |
| :---: | :---: | :---: |
| -2004 | 2 | 2 |
| -2008 | 1 | 1 |
| -2011 | 1 | 1 |
| -2015 | $(2,2)$ | 2 |
| -2019 | $(16,3)$ | 16 |
| -2020 | 4 | 2 |
| -2024 | $(2,7)$ | $(2,7)$ |
| -2027 | 1 | 1 |
| -2031 | 2 | 1 |
| -2035 | $(2,4)$ | $(2,4)$ |
| -2036 | 3 | 3 |
| -2039 | 2 | 1 |
| -2040 | $(2,2)$ | $(2,2)$ |
| -2047 | $(2,2)$ | 2 |
| -2051 | $(2,3)$ | $(2,3)$ |
| -2055 | $(2,2,3)$ | 2 |
| -2056 | 4 | 4 |
| -2059 | 2 | 2 |
| -2063 | 2 | 1 |
| -2067 | $(2,2)$ | $(2,2)$ |
| -2068 | 2 | 2 |
| -2071 | 2 | 1 |
| -2072 | 2 | 2 |
| -2083 | 1 | 1 |
| -2084 | 4 | 2 |
| -2087 | 2 | 1 |
| -2091 | $(2,2,3)$ | $(2,2)$ |
| -2095 | 2 | 1 |
| -2099 | 1 | 1 |
| -2103 | $(2,5)$ | 5 |
| -2104 | 2 | 2 |
| -2111 | 2 | 1 |
| -2119 | 2 | 1 |
| -2120 | 2 | 2 |
| -2123 | 2 | 2 |
| -2127 | $(2,3)$ | 1 |
| -2131 | 1 | 1 |
| -2132 | $(2,3)$ | $(2,3)$ |
| -2135 | $(2,2)$ | 2 |
| -2136 | $(2,3)$ | 2 |
| -2139 | $(2,2)$ | $(2,2)$ |
| -2143 | 2 | 1 |
| -2147 | 2 | 2 |
| -2148 | 4 | 2 |
| -2152 | 1 | 1 |
| -2155 | 2 | 2 |
| -2159 | $(2,2)$ | 2 |
| -2163 | $(2,2,3,5)$ | $(2,2,5)$ |
| -2164 | 1 | 1 |
| -2167 | 2 | 1 |
| -2168 | 2 | 2 |
|  |  |  |


| $d$ | tame | wild |
| :---: | :---: | :---: |
| -2171 | 2 | 2 |
| -2179 | 25 | 25 |
| -2180 | 4 | 2 |
| -2183 | $(2,3)$ | 3 |
| -2184 | $(2,2)$ | $(2,2)$ |
| -2191 | $(2,2)$ | 2 |
| -2195 | $(2,5)$ | $(2,5)$ |
| -2199 | $(2,3)$ | 1 |
| -2203 | 1 | 1 |
| -2207 | 2 | 1 |
| -2211 | $(2,8)$ | $(2,8)$ |
| -2212 | $(2,4)$ | $(2,2)$ |
| -2215 | $(2,5,23)$ | $(5,23)$ |
| -2216 | 1 | 1 |
| -2219 | 2 | 2 |
| -2227 | $(2,3)$ | $(2,3)$ |
| -2228 | 1 | 1 |
| -2231 | $(2,2)$ | 2 |
| -2235 | $(2,2,27)$ | $(2,2,9)$ |
| -2239 | 2 | 1 |
| -2243 | 1 | 1 |
| -2244 | $(2,8,3)$ | $(2,4)$ |
| -2247 | $(2,2)$ | 2 |
| -2248 | 2 | 2 |
| -2251 | 1 | 1 |
| -2255 | $(2,2)$ | 2 |
| -2260 | 2 | 2 |
| -2263 | $(2,2)$ | 2 |
| -2264 | 1 | 1 |
| -2267 | 1 | 1 |
| -2271 | $(2,3,5)$ | 5 |
| -2276 | 4 | 2 |
| -2279 | 2 | 1 |
| -2280 | $(2,2,3)$ | $(2,2)$ |
| -2283 | $(2,3)$ | $(2,3)$ |
| -2287 | 2 | 1 |
| -2291 | 2 | 2 |
| -2292 | 2 | 2 |
| -2296 | $(2,2)$ | $(2,2)$ |
| -2307 | $(4,3)$ | 4 |
| -2308 | 16 | 8 |
| -2311 | 2 | 1 |
| -2315 | 2 | 2 |
| -2319 | 2 | 1 |
| -2323 | 2 | 2 |
| -2324 | 2 | 2 |
| -2327 | 2 | 1 |
| -2328 | 4 | 4 |
| -2335 | 2 | 1 |
| -2339 | 1 | 1 |
| -2343 | $(2,2,3)$ | 2 |


| $d$ | tame | wild |
| :---: | :---: | :---: |
| -2344 | 3 | 3 |
| -2347 | 1 | 1 |
| -2351 | $(2,3)$ | 3 |
| -2355 | $(2,2,9)$ | $(2,2,9)$ |
| -2356 | 2 | 2 |
| -2359 | $(2,2)$ | 2 |
| -2360 | 2 | 2 |
| -2363 | 2 | 2 |
| -2371 | 1 | 1 |
| -2372 | 16 | 8 |
| -2379 | $(2,4,3)$ | $(2,4)$ |
| -2383 | 2 | 1 |
| -2387 | $(2,2)$ | $(2,2)$ |
| -2388 | $(2,3)$ | 2 |
| -2391 | 2 | 1 |
| -2392 | $(2,7)$ | $(2,7)$ |
| -2395 | $(2,25)$ | $(2,25)$ |
| -2399 | 2 | 1 |
| -2404 | 4 | 2 |
| -2407 | 2 | 1 |
| -2408 | $(2,3)$ | $(2,3)$ |
| -2411 | 1 | 1 |
| -2415 | $(2,2,2,3)$ | $(2,2)$ |
| -2419 | 4 | 4 |
| -2423 | 2 | 1 |
| -2424 | $(2,3)$ | 2 |
| -2427 | 2 | 2 |
| -2431 | $(2,2)$ | 2 |
| -2435 | 2 | 2 |
| -2436 | $(2,4)$ | $(2,2)$ |
| -2440 | 2 | 2 |
| -2443 | 2 | 2 |
| -2447 | $(2,7)$ | 7 |
| -2451 | $(2,4,3,7)$ | $(2,4,7)$ |
| -2452 | 1 | 1 |
| -2455 | 2 | 1 |
| -2456 | 1 | 1 |
| -2459 | 1 | 1 |
| -2463 | 2 | 1 |
| -2467 | 1 | 1 |
| -2468 | $(4,3)$ | $(2,3)$ |
| -2471 | $(2,2)$ | 2 |
| -2472 | 2 | 2 |
| -2479 | 2 | 1 |
| -2483 | 2 | 2 |
| -2487 | $(2,3)$ | 1 |
| -2488 | $(2,3)$ | $(2,3)$ |
| -2491 | $(2,3)$ | $(2,3)$ |
| -2495 | 2 | 1 |
| -2503 | 2 | 1 |
| -2504 | 2 | 2 |

Table 1. (Continued)

| $d$ | tame | wild | $d$ | tame | wild | $d$ | tame | wild |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -2507 | 2 | 2 | -2679 | $(2,2)$ | 2 | -2839 | (2, 2) | 2 |
| -2515 | 2 | 2 | -2680 | 2 | 2 | -2840 | 2 | 2 |
| -2516 | 2 | 2 | -2683 | 1 | 1 | -2843 | 1 | 1 |
| -2519 | 2 | 1 | -2687 | 2 | 1 | -2847 | $(2,2,3)$ | 2 |
| -2531 | 1 | 1 | -2692 | 8 | 4 | -2851 | , | 1 |
| -2532 | $(4,3)$ | 2 | -2696 | 8 | 8 | -2852 | $(2,4,3)$ | $(2,2,3)$ |
| -2536 | , | 1 | -2699 | 1 | 1 | -2855 | 2 | 1 |
| -2539 | 1 | 1 | -2703 | $(2,2,3)$ | 2 | -2856 | $(2,2,9)$ | $(2,2,3)$ |
| -2543 | 2 | 1 | -2707 | 1 | 1 | -2859 | $(2,5)$ | $(2,5)$ |
| -2551 | 2 | 1 | -2708 | 1 | 1 | -2863 | $(2,2)$ | 2 |
| -2552 | 2 | 2 | -2711 | 2 | 1 | -2867 | $(2,5)$ | $(2,5)$ |
| -2555 | $(2,2,3)$ | $(2,2,3)$ | -2712 | $(2,3)$ | 2 | -2868 | ) | 2 |
| -2559 | $(2,3)$ | 1 | -2715 | $(2,2)$ | $(2,2)$ | -2872 | 2 | 2 |
| -2563 | , | 2 | -2719 | , | , | -2879 | $(2,3)$ | 3 |
| -2564 | 8 | 4 | -2723 | 2 | 2 | -2884 | $(2,8)$ | $(2,4)$ |
| -2567 | $(2,2)$ | 2 | -2724 | 4 | 2 | -2887 | 2 | , |
| -2568 | $(2,3)$ | 2 | -2728 | 2 | 2 | -2895 | $(2,2)$ | 2 |
| -2571 | 2 | 2 | -2731 | 1 | 1 | -2899 | 2 | 2 |
| -2579 | 1 | 1 | -2735 | 2 | 1 | -2903 | 2 | 1 |
| -2580 | $(2,2)$ | $(2,2)$ | -2739 | $(2,8,3)$ | $(2,8)$ | -2911 | $(2,2)$ | 2 |
| -2584 | 8 | 8 | -2740 | $(2,3)$ | $(2,3)$ | -2915 | $(2,4,3)$ | $(2,4,3)$ |
| -2587 | 2 | 2 | -2743 | 2 | 1 | -2919 | $(2,4,3)$ | 4 |
| -2591 | 2 | 1 | -2747 | 2 | 2 | -2920 | 2 | 2 |
| -2595 | $(2,2,3)$ | $(2,2)$ | -2751 | $(2,4)$ | 4 | -2923 | $(2,3,23)$ | $(2,3,23)$ |
| -2596 | 4 | 2 | -2755 | $(2,2)$ | $(2,2)$ | -2927 | 2 | 1 |
| -2599 | $(2,2)$ | 2 | -2756 |  | 2 | -2931 | 2 | 2 |
| -2603 |  | 4 | -2759 | $(2,2,3)$ | $(2,3)$ | -2932 | 1 | 1 |
| -2607 | $(2,2)$ | 2 | -2760 | $(2,2)$ | $(2,2)$ | -2935 | 2 | 1 |
| -2611 | 2 | 2 | -2767 | $(2,5)$ | 5 | -2936 | 2 | 2 |
| -2612 | 1 | 1 | -2771 | 2 | 2 | -2939 | 1 | 1 |
| -2615 | 2 | 1 | -2776 | 11 | 11 | -2947 | 2 | 2 |
| -2616 | 2 | 2 | -2779 | 2 | 2 | -2948 | 4 | 2 |
| -2623 | 2 | 1 | -6787 | 2 | 2 | -2951 | $(2,5)$ | 5 |
| -2627 | $(2,3)$ | $(2,3)$ | -2788 | $(2,4)$ | $(2,2)$ | -2955 | $(2,2,3)$ | $(2,2)$ |
| -2631 | $(2,3)$ | 1 | -2791 | $(2,3)$ | , | -2959 | 2 | 1 |
| -2632 | $(2,2)$ | $(2,2)$ | -2792 | 5 | 5 | -2963 | 1 | 1 |
| -2635 | $(2,2)$ | $(2,2)$ | -2795 | $(2,2)$ | $(2,2)$ | -2964 | $(2,2,3)$ | $(2,2)$ |
| -2639 | $(2,2)$ | 2 | -2803 | 1 | 1 | -2967 | $(2,2)$ | 2 |
| -2643 | 2 | 2 | -2804 | 1 | 1 | -2968 | 2 | 2 |
| -2644 | 1 | 1 | -2807 | $(2,4)$ | 4 | -2971 | 5 | 5 |
| -2647 | 2 | 1 | -2811 | $(32,3)$ | 32 | -2980 | 4 | 2 |
| -2648 | 1 | 1 | -2815 | 2 | 1 | -2983 | 2 | 1 |
| -2651 | 2 | 2 | -2819 | 1 | 1 | -2984 | 1 | 1 |
| -2659 | 1 | 1 | -2820 | $(2,4,3)$ | $(2,2)$ | -2987 | 2 | 2 |
| -2660 | (2, 4) | $(2,2)$ | -2823 | 2 | 1 | -2991 | $(2,3)$ | 1 |
| -2663 | 2 | 1 | -2824 | $(8,3)$ | $(8,3)$ | -2995 | 2 | 2 |
| -2667 | $(2,2,3)$ | $(2,2)$ | -2827 | $(4,5)$ | $(4,5)$ | -2996 | 2 | 2 |
| -2671 | 2 | 1 | -2831 | 2 | 1 | -2999 | 2 | 1 |
| -2676 | $(2,3)$ | 2 | -2836 | 1 | 1 | -3003 | $(2,2,2)$ | (2, 2, 2) |

Table 1. (Continued)

| d | tame | wild | $d$ | tame | wild | d | tame | wild |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -3007 | (2, 4) | 4 | -3163 | 1 | 1 | -3335 | (2, 2) | 2 |
| -3011 | 7 | 7 | -3167 | 2 | 1 | -3336 | 2 | 2 |
| -3012 | 4 | 2 | -3171 | (2, 2, 3) | $(2,2)$ | -3343 | 2 | 1 |
| -3016 | 2 | 2 | -3172 | 4 | 2 | -3347 | 1 | 1 |
| -3019 | 7 | 7 | -3176 | 17 | 17 | -3351 | $(2,3)$ | 1 |
| -3023 | 2 | 1 | -3183 | 2 | 1 | -3352 | 1 | 1 |
| -3027 | $(4,3)$ | 4 | -3187 | 1 | 1 | -3355 | $(2,2,13)$ | $(2,2,13)$ |
| -3028 | 1 | 1 | -3188 | 1 | 1 | -3359 | $(2,3)$ | 3 |
| -3031 | $(2,2)$ | 2 | -3191 | 2 | 1 | -3363 | $(2,4)$ | (2, 4) |
| -3032 | 1 | 1 | -3192 | (2, 2) | $(2,2)$ | -3367 | $(2,2)$ | 2 |
| -3035 | 2 | 2 | -3199 | $(2,2)$ | 2 | -3368 | 1 | 1 |
| -3039 | 2 | 1 | -3203 | 1 | 1 | -3371 | 1 | 1 |
| -3043 | 4 | 4 | -3207 | $(2,3)$ | 1 | -3379 | $(2,37)$ | $(2,37)$ |
| -3044 | 4 | 2 | -3208 | 4 | 4 | -3383 | $(2,2)$ | 2 |
| -3047 | $(2,5)$ | 5 | -3215 | $(2,23)$ | 23 | -3387 | $(4,3,3)$ | $(4,3)$ |
| -3048 | $(2,5,9)$ | $(2,5,9)$ | -3219 | $(2,2)$ | $(2,2)$ | -3391 | 2 | 1 |
| -3055 | $(2,2,5)$ | $(2,5)$ | -3220 | (2, 2) | $(2,2)$ | -3395 | $(2,2)$ | $(2,2)$ |
| -3059 | $(2,2)$ | $(2,2)$ | -3223 | 2 | 1 | -3396 | $(4,3)$ | 2 |
| -3063 | $(2,3)$ | 1 | -3224 | (2, 7) | $(2,7)$ | -3399 | $(2,4)$ | 4 |
| -3064 | $(2,3)$ | $(2,3)$ | -3227 | 2 | 2 | -3403 | 8 | 8 |
| -3067 | 1 | 1 | -3235 | 2 | 2 | -3407 | 2 | 1 |
| -3071 | 2 | 1 | -3236 | 4 | 2 | -3412 | 1 | 1 |
| -3076 | 8 | 4 | -3239 | $(2,2)$ | 2 | -3415 | 2 | 1 |
| -3079 | 2 | 1 | -3243 | $(2,4,3)$ | $(2,4)$ | -3416 | $(2,11)$ | $(2,11)$ |
| -3080 | $(2,2)$ | $(2,2)$ | -3247 | $(2,16)$ | 16 | -3419 | 2 | 2 |
| -3083 | 1 | 1 | -3251 | 1 | 1 | -3423 | $(2,2,3,11)$ | $(2,11)$ |
| -3091 | 2 | 2 | -3252 | (2, 3) | 2 | -3427 | 2 | 2 |
| -3092 | 1 | 1 | -3255 | (2, 2, 2) | $(2,2)$ | -3428 | 4 | 2 |
| -3095 | 2 | 1 | -3256 | 2 | 2 | -3431 | $(2,2)$ | 2 |
| -3099 | $(4,3)$ | 4 | -3259 | 1 | 1 | -3432 | (2, 2, 3) | $(2,2)$ |
| -3103 | 2 | 1 | -3263 | 2 | 1 | -3435 | $(2,2)$ | $(2,2)$ |
| -3107 | 2 | 2 | -3268 | 4 | 2 | -3439 | 2 | 1 |
| -3108 | $(2,4,3,13)$ | $(2,2,13)$ | -3271 | (2, 3) | 3 | -3443 | 4 | 4 |
| -3111 | $(2,2)$ | 2 | -3272 | 2 | 2 | -3444 | $(2,2)$ | $(2,2)$ |
| -3112 | 1 | 1 | -3279 | (2, 3) | 1 | -3448 | 2 | 2 |
| -3115 | $(2,2)$ | $(2,2)$ | -3284 | 1 | 1 | -3451 | (2, 2, 3) | $(2,2,3)$ |
| -3119 | 2 | 1 | -3287 | 2 | 1 | -3455 | 2 | 1 |
| -3124 | 2 | 2 | -3288 | (2, 3) | 2 | -3459 | $(4,9)$ | $(4,3)$ |
| -3127 | 2 | 1 | -3291 | 2 | 2 | -3460 | 4 | 2 |
| -3128 | $(2,2)$ | $(2,2)$ | -3295 | 2 | 1 | -3463 | 2 | 1 |
| -3131 | 2 | 2 | -3299 | $(3,5)$ | $(3,5)$ | -3464 | 4 | 4 |
| -3135 | $(2,2,2,3)$ | $(2,2)$ | -3304 | 2 | 2 | -3467 | 1 | 1 |
| -3139 | 2 | 2 | -3307 | 1 | 1 | -3471 | (2, 2) | 2 |
| -3140 | 4 | 2 | -3311 | $(2,2)$ | 2 | -3476 | 2 | 2 |
| -3143 | $(2,2)$ | 2 | -3315 | (2, 2, 2, 3) | $(2,2,2)$ | -3480 | (2, 4) | $(2,4)$ |
| -3144 | $(2,3)$ | 2 | -3316 | 1 | 1 | -3487 | 2 | 1 |
| -3147 | 2 | 2 | -3319 | 2 | 1 | -3491 | 1 | 1 |
| -3151 | $(2,2)$ | 2 | -3320 | $(2,5)$ | $(2,5)$ | -3495 | (2, 2, 3) | 2 |
| -3155 | 2 | 2 | -3323 | 1 | 1 | -3496 | 2 | 2 |
| -3156 | 2 | 2 | -3327 | 2 | 1 | -3499 | 1 | 1 |
| -3160 | 2 | 2 | -3331 | 1 | 1 | -3503 | (2, 2) | 2 |

Table 1. (Continued)

| $d$ | tame | wild | $d$ | tame | wild | d | tame | wild |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| -3507 | $(2,2)$ | $(2,2)$ | -3659 | 1 | 1 | -3832 | 2 | 2 |
| -3508 | 1 | 1 | -3667 | 2 | 2 | -3835 | $(2,2,3,23)$ | $(2,2,3,23)$ |
| -3511 | 2 | 1 | -3668 | 2 | 2 | -3839 | 2 | , |
| -3512 | 2 | 2 | -3671 | $(2,3)$ | 3 | -3847 | 2 | 1 |
| -3515 | (2, 2) | $(2,2)$ | -3679 | 2 | 1 | -3848 | 2 | 2 |
| -3523 | 2 | 2 | -3683 | 2 | 2 | -3851 | 1 | 1 |
| -3524 | 16 | 8 | -3684 | $(4,3)$ | 2 | -3855 | $(2,2,3)$ | 2 |
| -3527 | 2 | 1 | -3687 | $(2,3)$ | 3 | -3859 | 2 | 2 |
| -3531 | $(2,4,3)$ | $(2,4)$ | -3688 | 1 | 1 | -3860 | 2 | 2 |
| -3535 | $(2,2)$ | 2 | -3691 | 1 | 1 | -3863 | 2 | 1 |
| -3539 | 1 | 1 | -3695 | $(2,3,5)$ | $(3,5)$ | -3864 | $(2,2,3)$ | $(2,2)$ |
| -3540 | $(2,2,27)$ | $(2,2,9)$ | -3704 | 2 | 2 | -3867 | 2 | 2 |
| -3543 | 2 | 1 | -3707 | 2 | 2 | -3876 | $(2,4)$ | $(2,2)$ |
| -3544 | 1 | 1 | -3711 | $(2,3)$ | 1 | -3880 | 2 | 2 |
| -3547 | 3 | 3 | -3715 | 2 | 2 | -3883 | 8 | 8 |
| -3551 | 2 | 1 | -3716 | 8 | 4 | -3891 | $(4,3)$ | 4 |
| -3556 | $(2,4)$ | $(2,2)$ | -3719 | 2 | 1 | -3892 | 2 | 2 |
| -3559 | 2 | 1 | -3720 | (2, 2, 3) | $(2,2)$ | -3895 | $(2,2)$ | 2 |
| -3560 | 4 | 4 | -3723 | $(2,2,5)$ | $(2,2,5)$ | -3896 | $(2,3)$ | $(2,3)$ |
| -3563 | 2 | 2 | -3727 | 2 | 1 | -3899 | $(2,3)$ | $(2,3)$ |
| -3567 | $(2,2,3)$ | 2 | -3731 | $(2,2)$ | $(2,2)$ | -3903 | 2 | 1 |
| -3571 | 1 | 1 | -3732 | 2 | 2 | -3907 | 1 | 1 |
| -3572 | 2 | 2 | -3736 | 1 | 1 | -3908 | 8 | 4 |
| -3576 | (2, 3) | 2 | -3739 | 1 | 1 | -3911 | 2 | 1 |
| -3579 | 2 | 2 | -3743 | 2 | 1 | -3912 | $(2,3)$ | $(2,3)$ |
| -3583 | 2 | 1 | -3747 | $(4,3)$ | 4 | -3919 | $(2,3)$ | 3 |
| -3587 | 2 | 2 | -7748 | 4 | 2 | -3923 | 1 | 1 |
| -3588 | $(2,4)$ | $(2,2)$ | -3752 | 2 | 2 | -3927 | (2, 2, 2, 3) | $(2,2)$ |
| -3592 | 4 | 4 | -3755 | 2 | 2 | -3928 | 1 | 1 |
| -3595 | 2 | 2 | -379 | $(2,2)$ | 2 | -3931 | 1 | 1 |
| -3599 | 2 | 1 | -3763 | $(2,3)$ | $(2,3)$ | -3935 | 2 | 1 |
| -3603 | $(4,3)$ | 4 | -3764 | 1 | 1 | -3939 | $(2,2)$ | $(2,2)$ |
| -3604 | $(4,3)$ | $(4,3)$ | -3767 | 2 | 1 | -3940 | 4 | 2 |
| -3607 | $(2,17)$ | 17 | -3768 | 2 | 2 | -3943 | $(2,3)$ | 3 |
| -3608 | 2 | 2 | -3779 | 1 | 1 | -3944 | 2 | 2 |
| -3611 | 2 | 2 | -3783 | $(2,2,9)$ | $(2,3)$ | -3947 | 1 | 1 |
| -3615 | $(2,4)$ | 4 | -3784 | 2 | 2 | -3955 | $(2,2)$ | $(2,2)$ |
| -3619 | $(2,2)$ | (2, 2) | -3787 | 2 | 2 | -3956 | $(2,5)$ | $(2,5)$ |
| -3620 | 4 | 2 | -3791 | $(2,4)$ | 4 | -3959 | $(2,23)$ | 23 |
| -3623 | 2 | 1 | -3795 | $(2,2,2)$ | $(2,2,2)$ | -3963 | $(8,3)$ | 8 |
| -3624 | $(2,125)$ | $(2,125)$ | -3796 | 2 | 2 | -3967 | 2 | 1 |
| -3631 | 2 | 1 | -3799 | 2 | 1 | -3972 | $(4,3)$ | 2 |
| -3635 | 2 | 2 | -3803 | 1 | 1 | -3976 | $(2,4)$ | $(2,4)$ |
| -3639 | $(2,3)$ | 1 | -3811 | 2 | 2 | -3979 | 2 | 2 |
| -3640 | $(2,4)$ | $(2,4)$ | -3812 | 4 | 2 | -3983 | $(2,2)$ | 2 |
| -3643 | 3 | 3 | -3815 | $(2,2)$ | 2 | -3988 | 1 | 1 |
| -3647 | $(2,2,3)$ | $(2,3)$ | -3819 | $(2,4,3)$ | $(2,4)$ | -3991 | 2 | 1 |
| -3651 | 2 | 2 | -3823 | 2 | 1 | -3992 | 1 | 1 |
| -3652 |  | 2 | -3827 | 2 | 2 | -3995 | $(2,2)$ | $(2,2)$ |
| -3655 | (2, 2) | 2 | -3828 | $(2,2,3)$ | $(2,2)$ | -3999 | $(2,4,9)$ | $(4,3)$ |
| -3656 | 2 | 2 | -3831 | 2 | 1 | -4003 | 1 | 1 |

Table 1. (Continued)

| $d$ | tame | wild |
| :---: | :---: | :---: |
| -4004 | $(2,4)$ | $(2,2)$ |
| -4007 | 2 | 1 |
| -4008 | $(2,3)$ | 2 |
| -4011 | $(2,2)$ | $(2,2)$ |
| -4015 | $(2,2)$ | 2 |
| -4019 | 5 | 5 |
| -4020 | $(2,2)$ | $(2,2)$ |
| -4024 | 2 | 2 |
| -4027 | 3 | 3 |
| -4031 | 2 | 1 |
| -4035 | $(2,2,3)$ | $(2,2)$ |
| -4036 | 8 | 4 |
| -4039 | $(2,2)$ | 2 |
| -4040 | 2 | 2 |
| -4043 | 2 | 2 |
| -4047 | $(2,2)$ | 2 |
| -4051 | 1 | 1 |
| -4052 | 1 | 1 |
| -4055 | 2 | 1 |
| -4063 | $(2,4)$ | 4 |
| -4071 | $(2,2,3)$ | 2 |
| -4072 | 3 | 3 |
| -4079 | 2 | 1 |
| -4083 | 2 | 2 |
| -4084 | 1 | 1 |
| -4087 | 2 | 1 |
| -4088 | $(2,2)$ | $(2,2)$ |
| -4091 | 1 | 1 |
| -4099 | 1 | 1 |
| -4103 | $(2,3)$ | 3 |
| -4111 | $(2,3)$ | 3 |
| -4115 | 2 | 2 |
| -4119 | $(2,3)$ | 3 |
| -4120 | 2 | 2 |
| -4123 | $(2,2)$ | $(2,2)$ |
| -4127 | 2 | 1 |
| -4132 | 4 | 2 |
| -4135 | 2 | 1 |
| -4136 | 2 | 2 |
| -4139 | 7 | 7 |
| -4143 | $(2,3)$ | 1 |
| -4147 | $(2,2,3)$ | $(2,2,3)$ |
| -4148 | $(2,29)$ | $(2,29)$ |
| -4151 | $(2,2,5)$ | $(2,5)$ |
| -4152 | $(2,3)$ | 2 |
| -4155 | $(2,2)$ | $(2,2)$ |
| -4159 | $(2,5)$ | 5 |
| -4163 | 2 | 2 |
| -4164 | 4 | 2 |
| -4168 | 2 | 2 |
| -4171 | 4 | 4 |


| $d$ | tame | wild |
| :---: | :---: | :---: |
| -4179 | $(2,2,3)$ | $(2,2)$ |
| -4180 | $(2,4)$ | $(2,4)$ |
| -4183 | $(2,4)$ | 4 |
| -4184 | 3 | 3 |
| -4187 | 2 | 2 |
| -4191 | $(2,2)$ | 2 |
| -4195 | 2 | 2 |
| -4196 | 4 | 2 |
| -4199 | $(2,4)$ | 4 |
| -4207 | $(2,2)$ | 2 |
| -4211 | 1 | 1 |
| -4215 | $(2,2,3)$ | 2 |
| -4216 | $(2,2)$ | $(2,2)$ |
| -4219 | 3 | 3 |
| -4223 | $(2,4)$ | 4 |
| -4227 | 2 | 2 |
| -4228 | $(2,8)$ | $(2,4)$ |
| -4231 | 2 | 1 |
| -4243 | 5 | 5 |
| -4244 | 5 | 5 |
| -4247 | $(2,2)$ | 2 |
| -4251 | $(2,4,3,7)$ | $(2,4,7)$ |
| -4255 | $(2,2,3)$ | $(2,3)$ |
| -4259 | 1 | 1 |
| -4260 | $(2,4,3)$ | $(2,2)$ |
| -4264 | 2 | 2 |
| -4267 | 4 | 4 |
| -4271 | 2 | 1 |
| -4276 | 1 | 1 |
| -4279 | 2 | 1 |
| -4280 | 2 | 2 |
| -4283 | 3 | 3 |
| -4287 | $(2,3)$ | 1 |
| -4291 | 2 | 2 |
| -4292 | 4 | 2 |
| -4295 | 2 | 1 |
| -4296 | $(2,3)$ | 2 |
| -4299 | 2 | 2 |
| -4303 | 2 | 1 |
| -4307 | $(2,5)$ | $(2,5)$ |
| -4308 | $(2,3)$ | $(2,3)$ |
| -4315 | 2 | 2 |
| -4319 | $(2,4,5)$ | $(4,5)$ |
| -4323 | $(2,4,3)$ | $(2,4)$ |
| -4324 | $(2,4)$ | $(2,2)$ |
| -4327 | 2 | 1 |
| -4328 | 1 | 1 |
| -4331 | $(2,7)$ | $(2,7)$ |
| -4339 | 1 | 1 |
| -4340 | $(2,2)$ | $(2,2)$ |
| -4343 | 2 | 1 |


| $d$ | tame | wild |
| :---: | :---: | :---: |
| -4344 | 2 | 2 |
| -4351 | 2 | 1 |
| -4355 | $(2,2)$ | $(2,2)$ |
| -4359 | $(2,3)$ | 1 |
| -4360 | 2 | 2 |
| -4363 | 3 | 3 |
| -4367 | 2 | 1 |
| -4371 | $(2,2,49)$ | $(2,2,49)$ |
| -4372 | 1 | 1 |
| -4376 | 1 | 1 |
| -4379 | 2 | 2 |
| -4387 | 8 | 8 |
| -4388 | 4 | 2 |
| -4391 | 2 | 1 |
| -4395 | $(2,2,3)$ | $(2,2)$ |
| -4399 | 2 | 1 |
| -4403 | $(2,2)$ | $(2,2)$ |
| -4404 | $(2,3)$ | 2 |
| -4407 | $(2,2)$ | 2 |
| -4408 | 2 | 2 |
| -4411 | 4 | 4 |
| -4415 | $(2,3,7)$ | $(3,7)$ |
| -4420 | $(2,4)$ | $(2,2)$ |
| -4423 | $(2,3)$ | 3 |
| -4424 | $(2,2,5)$ | $(2,2,5)$ |
| -4427 | 4 | 4 |
| -4431 | $(2,2,3)$ | 2 |
| -4435 | 2 | 2 |
| -4436 | 1 | 1 |
| -4439 | $(2,2)$ | 2 |
| -4440 | $(2,2,3)$ | $(2,2)$ |
| -4443 | 2 | 2 |
| -4447 | 2 | 1 |
| -4451 | 1 | 1 |
| -4452 | $(2,4)$ | $(2,2)$ |
| -4456 | 1 | 1 |
| -4463 | 2 | 1 |
| -4467 | $(4,3)$ | 4 |
| -4468 | 1 | 1 |
| -4471 | $(2,2)$ | 2 |
| -4472 | 2 | 2 |
| -4479 | 2 | 1 |
| -4483 | 1 | 1 |
| -4484 | 4 | 2 |
| -4487 | $(2,4)$ | 4 |
| -4488 | $(2,4)$ | $(2,4)$ |
| -4495 | $(2,2)$ | 2 |
| -4499 | 2 | 2 |
| -4503 | $(2,2,3)$ | 2 |
| -4504 | 1 | 1 |
| -4507 | 1 | 1 |
|  |  |  |

Table 1. (Continued)

| $d$ | tame | wild |
| :---: | :---: | :---: |
| -4511 | 2 | 1 |
| -4515 | $(2,2,2)$ | $(2,2,2)$ |
| -4516 | 4 | 2 |
| -4519 | 2 | 1 |
| -4520 | 2 | 2 |
| -4523 | 1 | 1 |
| -4531 | 2 | 2 |
| -4532 | 2 | 2 |
| -4535 | 2 | 1 |
| -4539 | $(2,2,3)$ | $(2,2)$ |
| -4543 | $(2,2)$ | 2 |
| -4547 | 233 | 233 |
| -4548 | $(4,3)$ | 2 |
| -4551 | $(2,2)$ | 2 |
| -4552 | 2 | 2 |
| -4555 | 2 | 2 |
| -4559 | $(2,2)$ | 2 |
| -4564 | 2 | 2 |
| -4567 | 2 | 1 |
| -4568 | 1 | 1 |
| -4571 | 2 | 2 |
| -4579 | $(2,5)$ | $(2,5)$ |
| -4580 | 4 | 2 |
| -4583 | $(2,5)$ | 5 |
| -4584 | $(2,3)$ | 2 |
| -4587 | $(2,2)$ | $(2,2)$ |
| -4591 | 2 | 1 |
| -4595 | $(2,3)$ | $(2,3)$ |
| -4596 | 2 | 2 |
| -4603 | 1 | 1 |
| -4607 | $(2,4)$ | 4 |
| -4611 | $(2,2,3)$ | $(2,2)$ |
| -4612 | 8 | 4 |
| -4615 | $(2,2)$ | 2 |
| -4616 | 8 | 8 |
| -4619 | 2 | 2 |
| -4623 | $(2,2)$ | 2 |
| -4627 | 2 | 2 |
| -4628 | 2 | 2 |
| -4631 | 2 | 1 |
| -4632 | $(4,7)$ | $(4,7)$ |
| -4639 | 2 | 1 |
| -4643 | 1 | 1 |
| -4647 | $(2,3)$ | 1 |
| -4648 | 2 | 2 |
| -4651 | 1 | 1 |
| -4659 | 2 | 2 |
| -4660 | 2 | 2 |
| -4663 | 2 | 1 |
| -4664 | 2 | 2 |
| -4667 | 2 | 2 |


| $d$ | tame | wild |
| :---: | :---: | :---: |
| -4676 | $(2,8)$ | $(2,4)$ |
| -4679 | 2 | 1 |
| -4683 | $(2,2,3,37)$ | $(2,2,37)$ |
| -4687 | 2 | 1 |
| -4691 | 1 | 1 |
| -4692 | $(2,2,3)$ | $(2,2)$ |
| -4695 | $(2,2)$ | 2 |
| -4696 | 1 | 1 |
| -4699 | 2 | 2 |
| -4703 | 2 | 1 |
| -4708 | 4 | 2 |
| -4711 | $(2,2)$ | 2 |
| -4712 | 2 | 2 |
| -4715 | $(2,4)$ | $(2,4)$ |
| -4723 | 1 | 1 |
| -4724 | 1 | 1 |
| -4727 | 2 | 1 |
| -4728 | $(2,3)$ | 2 |
| -4731 | $(2,2)$ | $(2,2)$ |
| -4735 | 2 | 1 |
| -4739 | 2 | 2 |
| -4740 | $(2,4)$ | $(2,2)$ |
| -4744 | 8 | 8 |
| -4747 | 2 | 2 |
| -4751 | 2 | 1 |
| -4755 | $(2,2,3)$ | $(2,2)$ |
| -4756 | 2 | 2 |
| -4759 | 2 | 1 |
| -4760 | $(2,2)$ | $(2,2)$ |
| -4763 | 4 | 4 |
| -4767 | $(2,4)$ | 4 |
| -4771 | $(2,7)$ | $(2,7)$ |
| -4772 | $(4,3,5)$ | $(2,3,5)$ |
| -4776 | 2 | 2 |
| -4783 | $(2,5)$ | 5 |
| -4787 | 1 | 1 |
| -4791 | $(2,3)$ | 1 |
| -4792 | $(2,9)$ | $(2,9)$ |
| -4795 | $(2,2,3,7)$ | $(2,2,3,7)$ |
| -4799 | $(2,3)$ | 3 |
| -4803 | 2 | 2 |
| -4804 | 8 | 4 |
| -4807 | $(2,4)$ | 4 |
| -4808 | $(2,3)$ | $(2,3)$ |
| -4811 | 2 | 2 |
| -4819 | $(2,3)$ | $(2,3)$ |
| -4820 | 4 | 4 |
| -4823 | $(2,2)$ | 2 |
| -4827 | $(4,9)$ | $(4,3)$ |
| -4831 | 2 | 1 |
| -4835 | $(2,3)$ | $(2,3)$ |


| $d$ | tame | wild |
| :---: | :---: | :---: |
| -4836 | $(2,4,3)$ | $(2,2)$ |
| -4839 | 2 | 1 |
| -4843 | 2 | 2 |
| -4847 | 2 | 1 |
| -4852 | 1 | 1 |
| -4855 | 2 | 1 |
| -4856 | 2 | 2 |
| -4859 | 2 | 2 |
| -4863 | $(2,3)$ | 1 |
| -4867 | 2 | 2 |
| -4868 | 64 | 32 |
| -4871 | 2 | 1 |
| -4872 | $(2,2,3)$ | $(2,2)$ |
| -4879 | $(2,2,2)$ | $(2,2)$ |
| -4883 | 2 | 2 |
| -4884 | $(2,16)$ | $(2,16)$ |
| -4888 | $(2,5,7)$ | $(2,5,7)$ |
| -4891 | 4 | 4 |
| -4895 | $(2,4)$ | 4 |
| -4899 | $(2,8,3)$ | $(2,8)$ |
| -4903 | $(2,5)$ | 5 |
| -4904 | 1 | 1 |
| -4907 | 2 | 2 |
| -4911 | 2 | 1 |
| -4915 | 2 | 2 |
| -4916 | 1 | 1 |
| -4919 | 2 | 1 |
| -4920 | $(2,2)$ | $(2,2)$ |
| -4927 | 2 | 1 |
| -4931 | 1 | 1 |
| -4935 | $(2,2,3)$ | $(2,2)$ |
| -4936 | $(2,5)$ | $(2,5)$ |
| -4939 | 4 | 4 |
| -4943 | 2 | 1 |
| -4947 | $(2,2)$ | $(2,2)$ |
| -4948 | 17 | 17 |
| -4951 | 2 | 1 |
| -4952 | 1 | 1 |
| -4955 | 2 | 2 |
| -4963 | 2 | 2 |
| -4964 | $(2,4)$ | $(2,2)$ |
| -4967 | 2 | 1 |
| -4971 | $(16,3)$ | 16 |
| -4979 | 2 | 2 |
| -4980 | $(2,2,3)$ | $(2,2)$ |
| -4983 | $(2,2)$ | 2 |
| -4984 | $(2,2)$ | $(2,2)$ |
| -4987 | 1 | 1 |
| -4991 | $(2,2,2)$ | $(2,2)$ |
| -4996 | 32 | 16 |
| -4999 | 2 | 1 |

## References

[BBCO] C. Bernardi. D. Batut, H. Cohen and M. Olivier, GP-PARI, a computer package.
[Bl] S. Bloch, Applications of the dilogarithm function in algebraic $K$-theory and algebraic geometry, Proc. Int. Symp. Alg. Geom., Kyoto, Kinokuniya, 1977, pp. 103-114. MR 82f:14009
[Bo1] A. Borel, Cohomologie de $S L_{n}$ et valeurs de fonctions zêta aux points entiers, Ann. Sc. Norm. Sup. Pisa (4) 4, no. 4 (1977), 613-636; errata 7, no. 2 (1980), 373. MR 58:22016; MR 81k:12012
[Bo2] A. Borel, Values of zeta-functions at integers, cohomology and polylogarithms, Current Trends in Mathematics and Physics, 1-44, Narosa, New Delhi, 1995. MR 97a:19005
[B-82] J. Browkin, The functor $K_{2}$ for the ring of integers of a number field, Universal Algebra and Applications, (Warsaw, 1978), Banach Center Publications, vol. 9, PWN, Warsaw, 1982, pp. 187-195. MR 85f:11084
[B-92] J. Browkin, On the p-rank of the tame kernel of algebraic number fields, Journ. Reine Angew. Math., 432 (1992), 135-149. MR 93j:11077
[B-S] J. Browkin and A. Schinzel, On Sylow 2-subgroups of $K_{2} O_{F}$ for quadratic number fields $F$, Journ. Reine Angew. Math., 331 (1982), 104-113. MR 83g: 12011
[C-H] P. E. Conner and J. Hurrelbrink, Class number parity, Series in Pure Math. 8, World Scientific Publ, Singapore, 1988. MR 90f:11092
[Ga] H. Gangl, Werte von Dedekindschen Zetafunktionen, Dilogarithmuswerte und Pflasterungen des hyperbolischen Raumes, Diplomarbeit Bonn, 1989.
[Gr] D. Grayson, Dilogarithm computations for $K_{3}$ in: Algebraic K-theory, Evanston 1980 (Proc. Conf., Northwestern Univ., Evanston, Ill., 1980), Lecture Notes in Math. 854 (1981), 168-178. MR 82i:12012
[KNF] M. Kolster, T. Nguyen Quang Do, V. Fleckinger, Twisted S-units, p-adic class number formulas, and the Lichtenbaum conjectures, Duke Math. J., 84 (1996), 679-717; errata 90 (1997), 641-643. MR 97g:11136; CMP 98:04
[Li] S. Lichtenbaum, Values of zeta-functions, étale cohomology, and algebraic K-theory, Lecture Notes in Math. 342 (1973), 489-501 Springer, Berlin. MR 53:10765
[M-W] B. Mazur, A. Wiles, Class fields of abelian extensions of $\mathbb{Q}$, Invent. Math. 76, no. 2 (1984), 179-330. MR 85m:11069
[Q1] Qin Hourong, The 2-Sylow subgroups of the tame kernel of imaginary quadratic fields, Acta Arith., 69 (1995), 153-169. MR 96a:11132
[Q2] Qin Hourong, Computation of $K_{2} Z[\sqrt{-6}]$, Journ. Pure Appl. Algebra 96 (1994), 133-146. MR 95i:11135
[Q3] Qin Hourong, Computation of $K_{2} Z\left[\frac{1+\sqrt{-35}}{2}\right]$, Chin. Ann. of Math., 17B, 1 (1996), 63-72. MR 97a:19004
[Sk] M. Skałba, Generalization of Thue's theorem and computation of the group $K_{2} O_{F}$, J. Number Theory 46 (1994), 303-322. MR 95d:19001
[Su] A.A. Suslin, Algebraic K-theory of fields, in: Proceedings of the International Congress of Mathematicians, Berkeley, CA, 1986, Vol.I, AMS, Providence, RI, 1987, pp. 222-244. MR 89k:12010
[Ta] J. Tate, Appendix to "The Milnor ring of a global field" by H. Bass and J. Tate in: Algebraic K-theory, II: "Classical" algebraic K-theory and connections with arithmetic (Proc. Conf., Seattle Res. Center, Battelle Memorial Inst., 1971), Lecture Notes in Math. 342 (1973), 429-446. MR 56:449

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